



**Ph.D. Incoming Erasmus Student Seminar  
at Computer Vision & Multimedia Lab,  
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# **Depth Estimation using Single Digital Still Camera & 2D Real-Time Video Stabilization**

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# Content

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## PART 1

### Depth Estimation using Single Digital Still Camera

|  |    |
|--|----|
| 1.1. Introduction .....  | 3  |
| 1.2. Geometrical Model of a Canonical Stereovision Configuration ..... | 4  |
| 1.3. Depth Resolution of a C.S.C. ....                                 | 5  |
| 1.4. Depth Estimation Algorithm .....                                  | 6  |
| 1.4.1. Corners Detection (Examples) .....                              | 7  |
| 1.4.2. Searching for Matches (Examples) .....                          | 10 |
| 1.5. Experimental Results .....  | 13 |
| 1.5.1. Depth Estimation to Definite Points (Olympus) .....             | 15 |
| 1.5.2. Depth Estimation to Definite Points (Kodak) .....               | 18 |
| 1.6. Conclusion and Future Work .....                                  | 21 |

## PART 2

### 2D Real-Time Video Stabilization

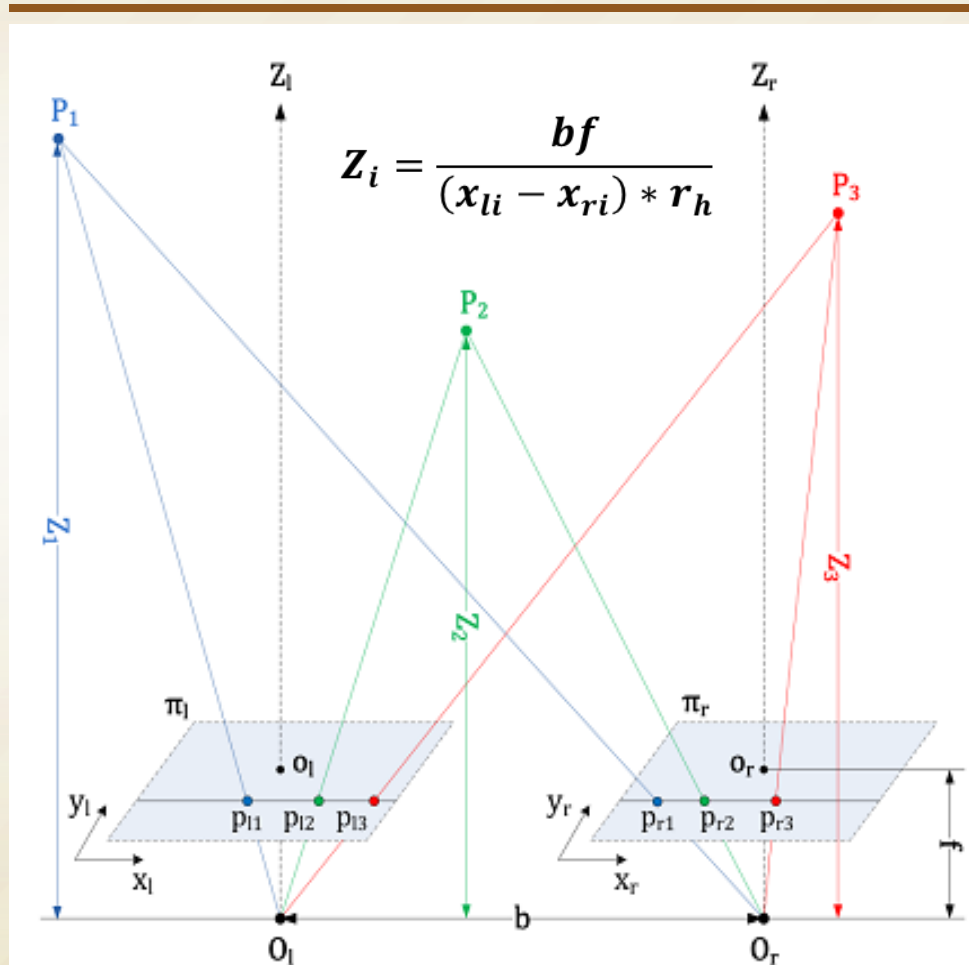
|   |    |
|---|----|
| 2.1. Introduction .....                     | 23 |
| 2.2. 2D Video Stabilization Algorithm ..... | 24 |
| 2.3. Motion Vectors Model .....             | 25 |
| 2.4. SAD examples .....                     | 28 |
| 2.5. Live Demo .....                        | 30 |
| 2.6. Conclusion .....                       | 31 |

# Depth Estimation using Single Digital Still Camera

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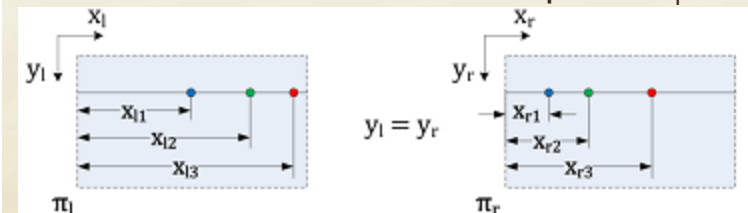
- The present work's objective is to investigate the possibilities of a simple method for acquiring the depth using the principles of a canonical stereo vision system.
- The aim is to prove by physical experiments, using conventional digital still camera, when a real stereovision system is not available, is possible to effectively determine the depth to particular object points in a given static scene.
- The main requirement is that the camera should have precise horizontal movement, high resolution and possibilities for adjusting the parameters of its optical system.

# Geometrical Model of a Canonical Stereovision Configuration



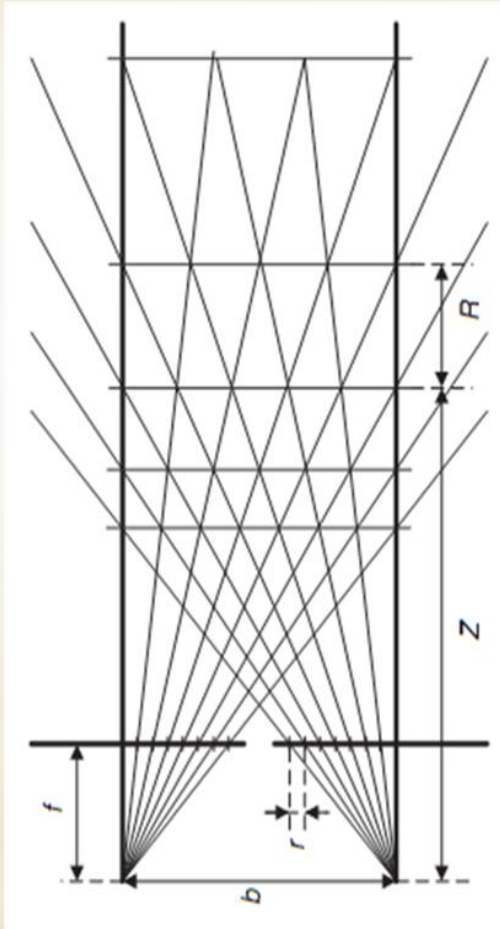
## Parameters of a CSC:

(1)  $O_l$  and  $O_r$  - optical centers of the cameras; (2)  $Z_l$  and  $Z_r$  - parallel principal axes that pass through points  $O_l$  and  $O_r$  which are perpendicular to the image planes  $\pi_l$  and  $\pi_r$ ; (3) **base length,  $b$**  - the distance between the points  $O_l$  and  $O_r$ ; (4) **focal length,  $f$**  - the distance from the image planes to the central points  $O_l$  and  $O_r$ ; (5)  $p_{li}$  and  $p_{ri}$  - the projections of an arbitrary point  $P_i$  within the scene on the image planes  $\pi_l$  and  $\pi_r$ ; (6)  **$x_{li}$  and  $x_{ri}$**  - distances, measured from the top left corner of the images to the corresponding projections of a given point  $P_i$  ( $p_{li}$  and  $p_{ri}$ ); (7)  **$Z_i$**  - the distance between the line connecting the optical centers of the cameras and the scene point  $P_i$ .



Geometrical model of a canonical stereo configuration

# Depth Resolution of a Canonical Stereovision System



The phenomenon of diminishing accuracy of depth measurement with increasing distance from the camera planes is a geometrical limitation since it depends exclusively on geometrical parameters of a stereovision system.

$$R \approx \frac{rZ^2}{fb}$$

For most image acquisition systems, the values of  $r$ ,  $b$  and  $f$  are constant, at least for a single acquisition. This means that there is such a value  $Z$  for which it is not possible to measure the depth of the observed scene due to geometrical limitations of a stereovision setup.

# Depth Estimation Algorithm

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The main problem in determining the distance to objects in a scene from a pair of stereo images, obtained by a canonical stereo configuration, is to find pairs of corresponding image points, which represent projection of one point from a 3D scene.

**Step 1: Features detection** in the stereo images by cornerness measure, proposed by Alison Noble, on the basis of the Harris corner detector.

**Step 2: Searching for matches** by the method *Sum of Absolute Differences* between the previously found feature points (corners).

**Step 3: Depth estimation** using the relationship between disparity, base length and focal length, obtained on the basis of the geometrical model of a canonical stereo configuration.



# Corners Detection

## Harris cornerness measure

$$C(x,y) = \det(M) - k(\text{trace}(M))^2$$

where  $k = 0.04 \div 0.06$

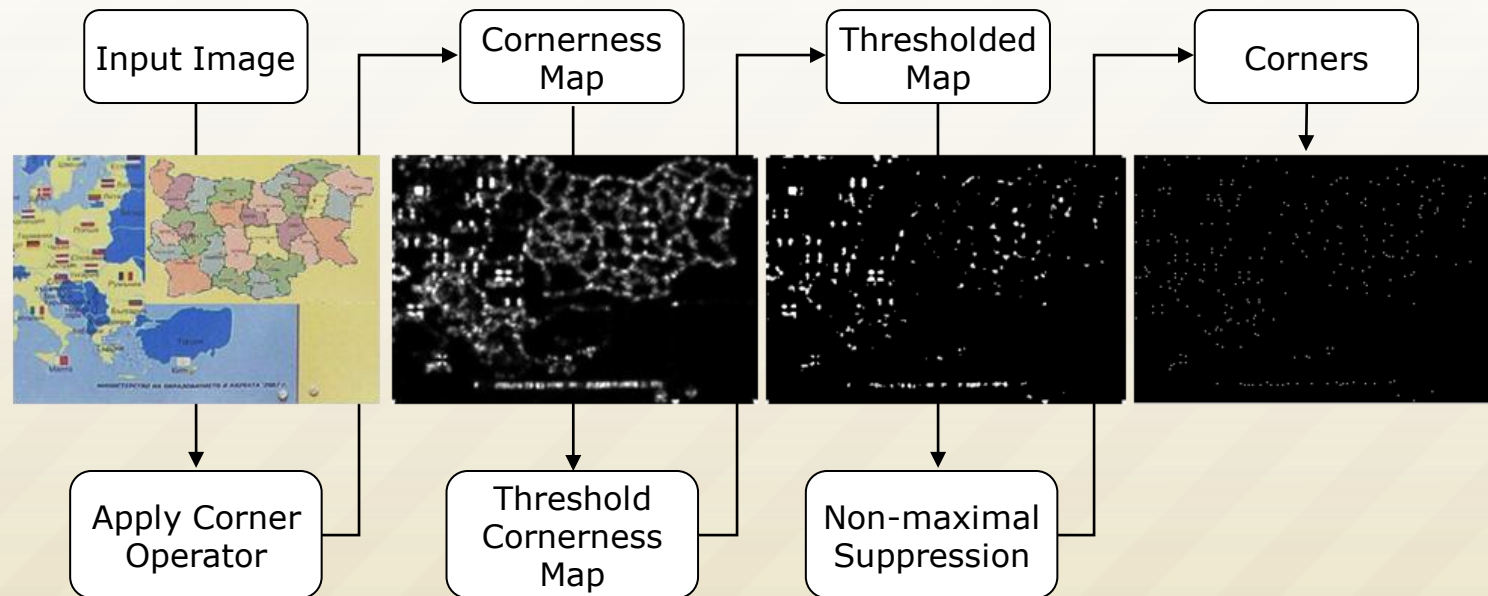
$$M = \begin{bmatrix} A & C \\ C & B \end{bmatrix}, \det(M) = AB - C^2, \text{trace}(M) = A + B, A = I_x^2 \otimes w, B = I_y^2 \otimes w, C = I_x I_y \otimes w$$

$\otimes$  is the convolution operator,  
 $w$  is the Gaussian window

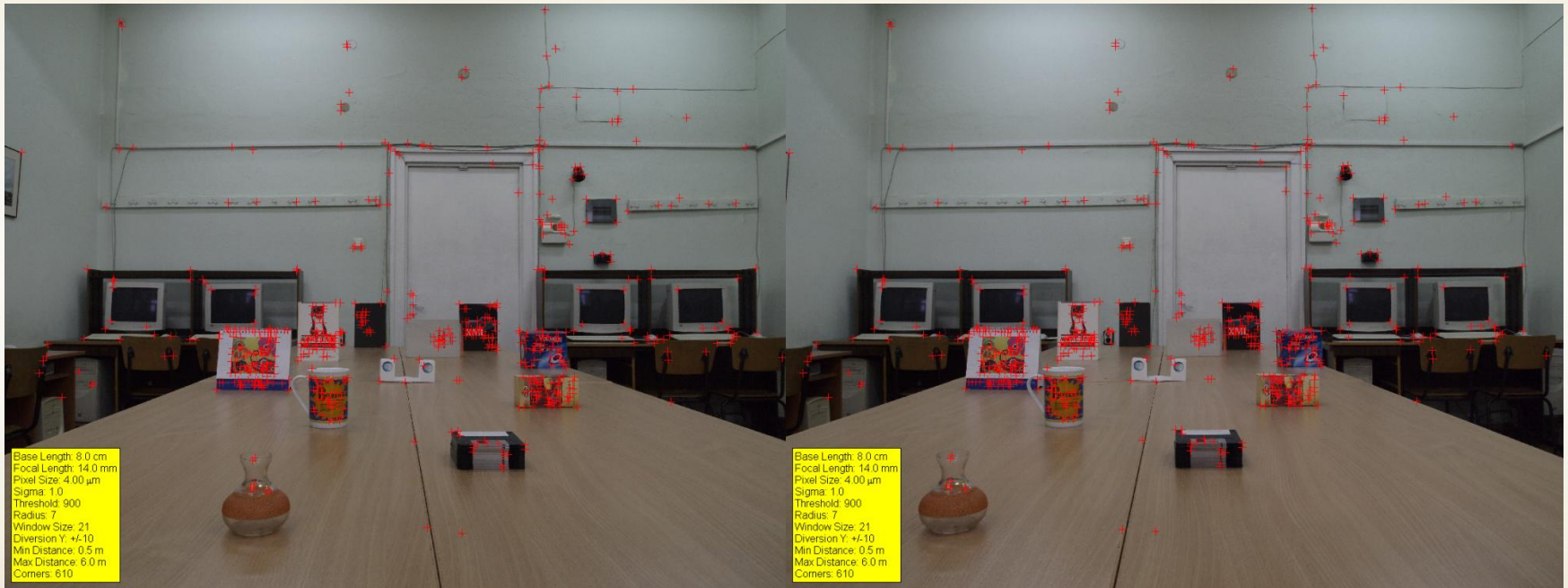
$$I_x = I \otimes (-1, 0, 1) \approx \frac{dI}{dx} \text{ and } I_y = I \otimes (-1, 0, 1)^T \approx \frac{dI}{dy}$$

## A. Noble cornerness measure

$$C(x,y) = \det(M) / \text{trace}(M)$$



# An Example of Found Corners in a Pair of Stereo Images



(Olympus)



# An Example of Found Corners in a Pair of Stereo Images



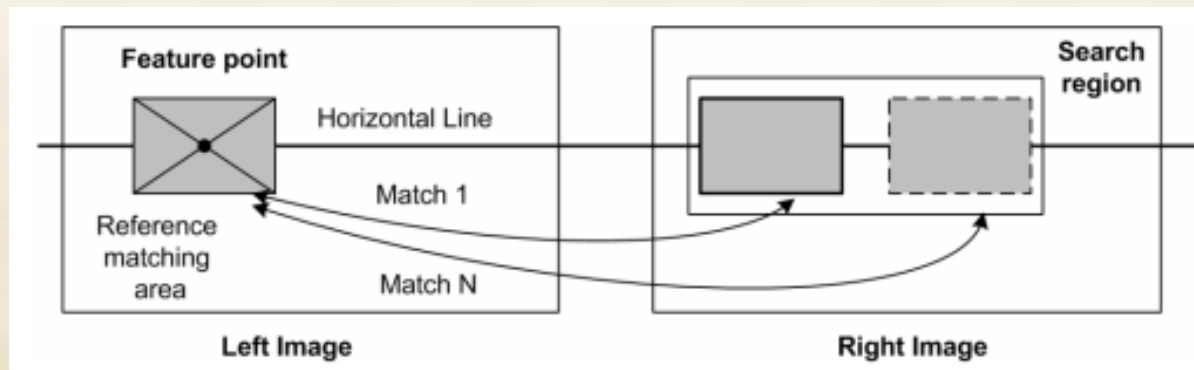
(Kodak)

# Searching for Matches

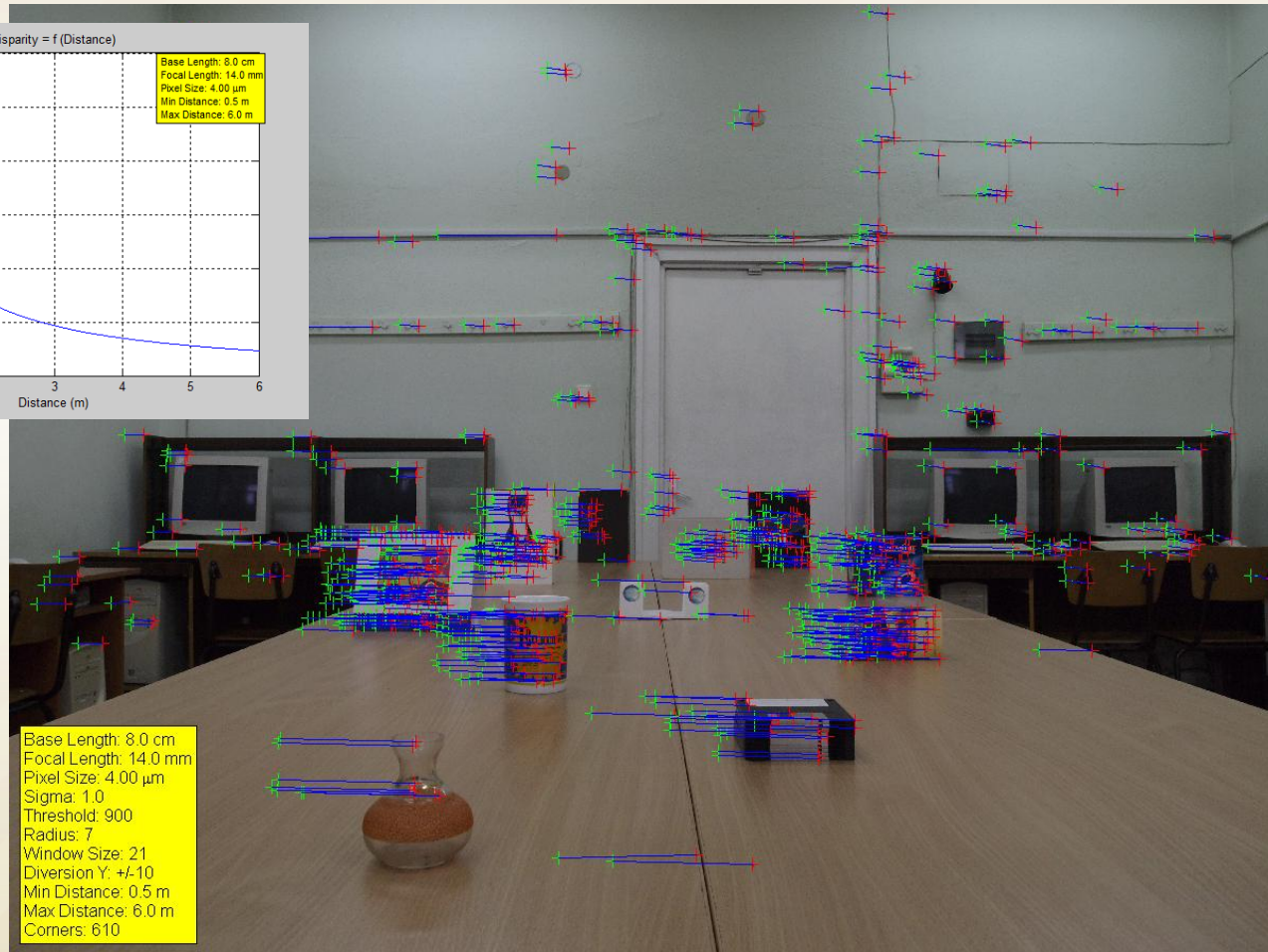
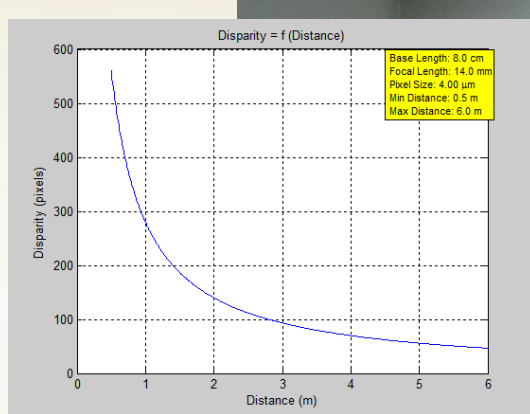
The metric used to determine which features in the stereo pair correspond to each other is based on *Sum of Absolute Differences*:

$$SAD = \sum_{(i,j) \in U} |I_1(x + i, y + j) - I_2(x + d_x + i, y + d_y + j)|$$

where:  $I_1$  and  $I_2$  are two image regions being compared. The region  $I_1$  is built around a reference point  $(x, y)$ , and the region  $I_2$  - around point  $(x + d_x, y + d_y)$ , where with  $d_x$  and  $d_y$  are denoted the relative horizontal and vertical displacements of the two image blocks being compared. The matching regions are defined by a set  $U$  of offset values, measured from their reference points, i.e.  $(x, y)$  and  $(x + d_x, y + d_y)$ , respectively.



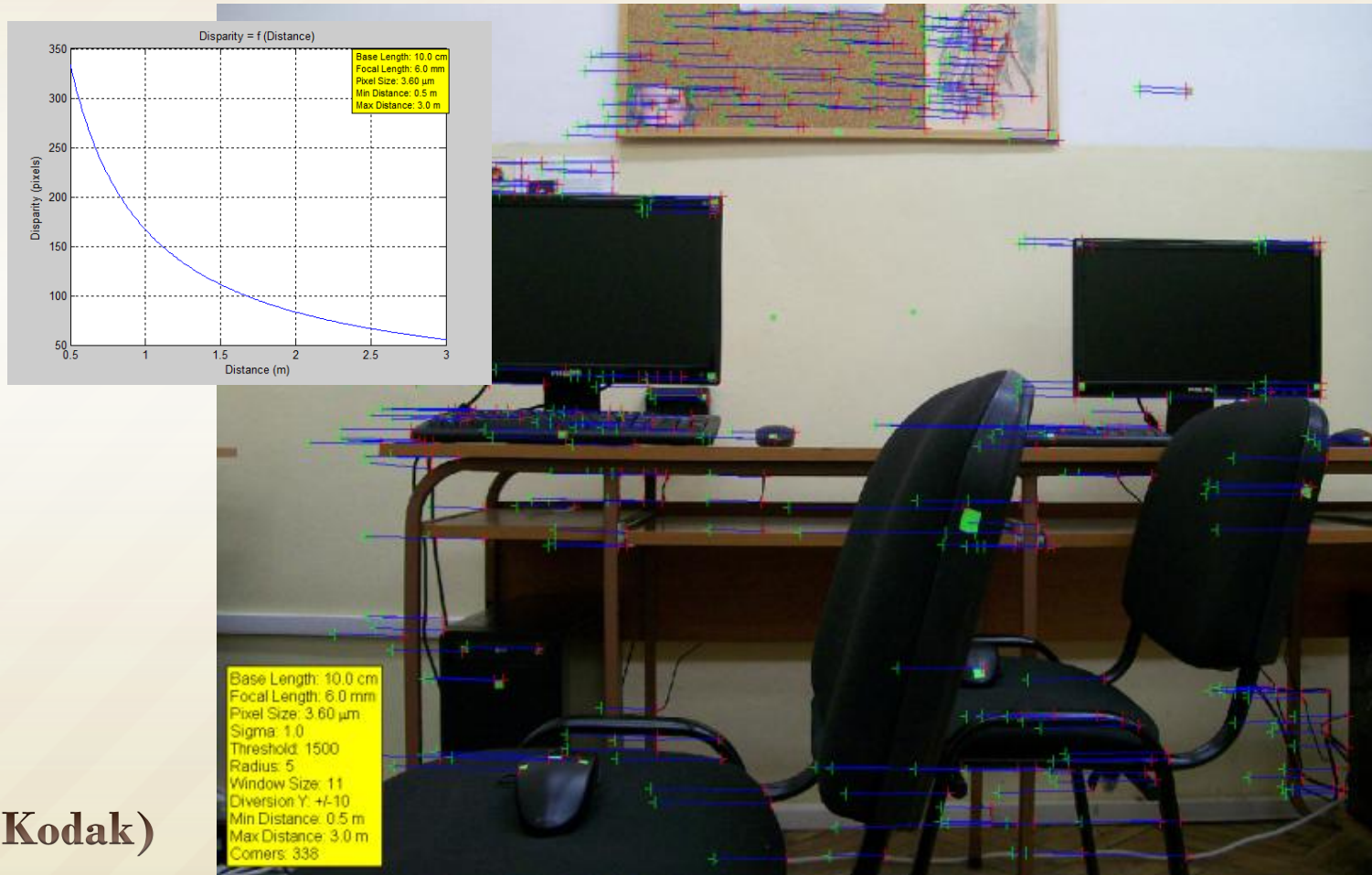
# An Example of Found Correspondences Between Previously Detected Corners



(Olympus)



# An Example of Found Correspondences Between Previously Detected Corners

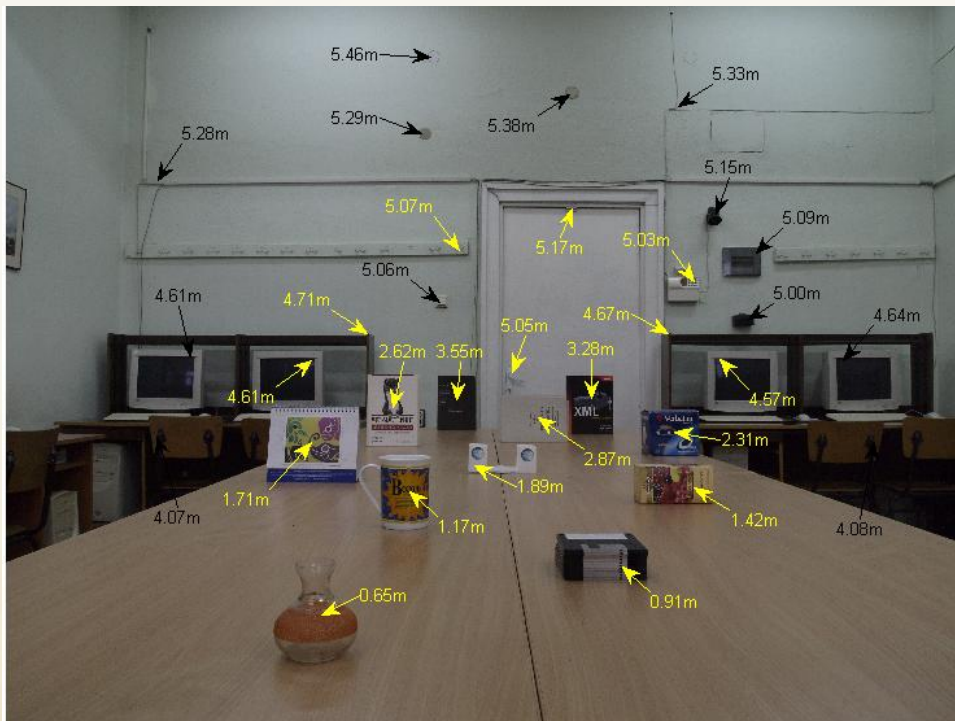


(Kodak)

# Experimental Results

Our experimental work has two goals:

- 1)** to verify the applicability of the mathematical model, using a non-real stereovision system;
- 2)** to test the accuracy of the estimated distances in a real static scene.



Real Distances to selected objects (Olympus)



Experimental Platform



Laser distancemeter



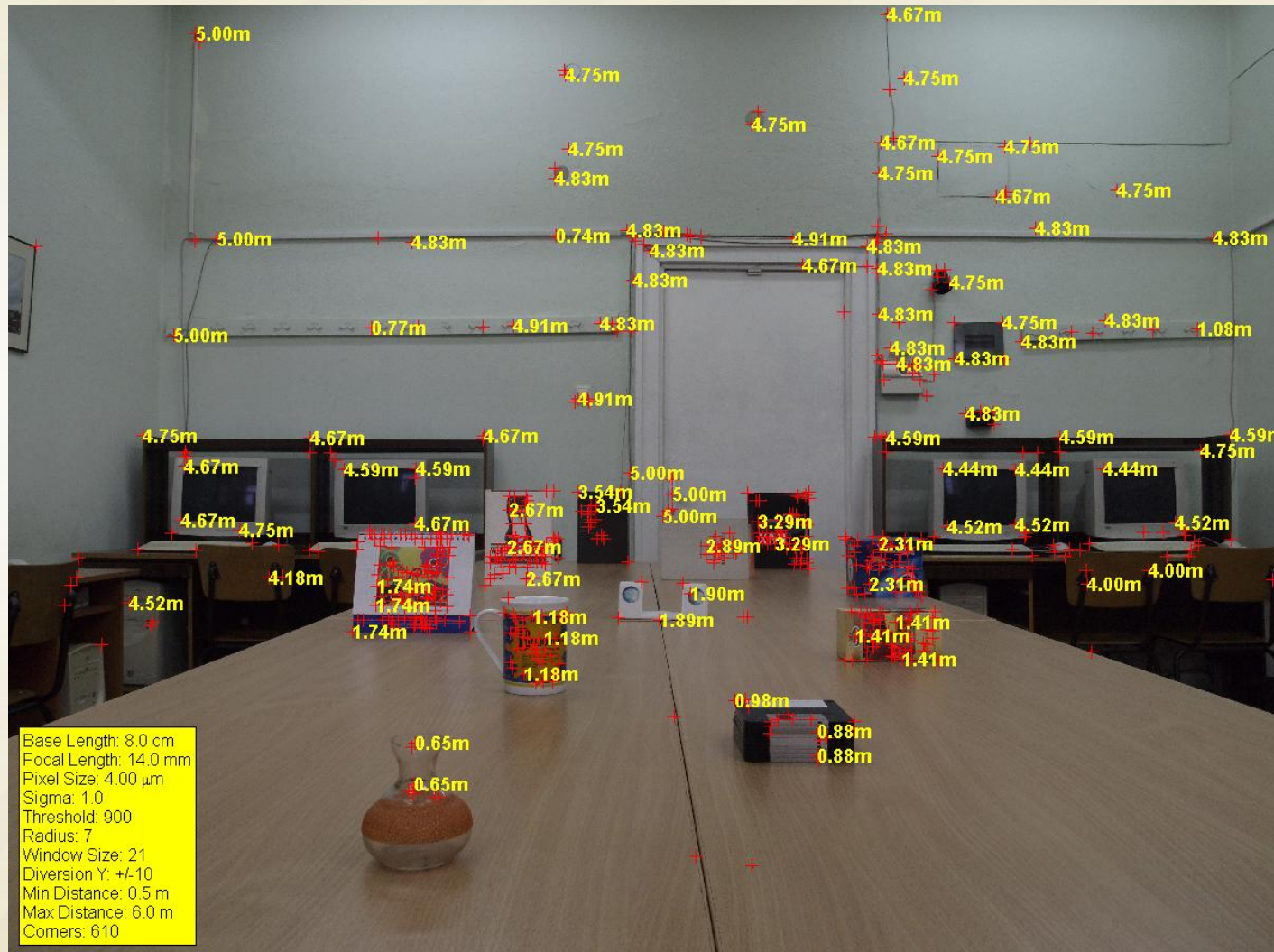
# Experimental Results



Real Distances to selected objects (Kodak) – unprofessional, but effective method ☺

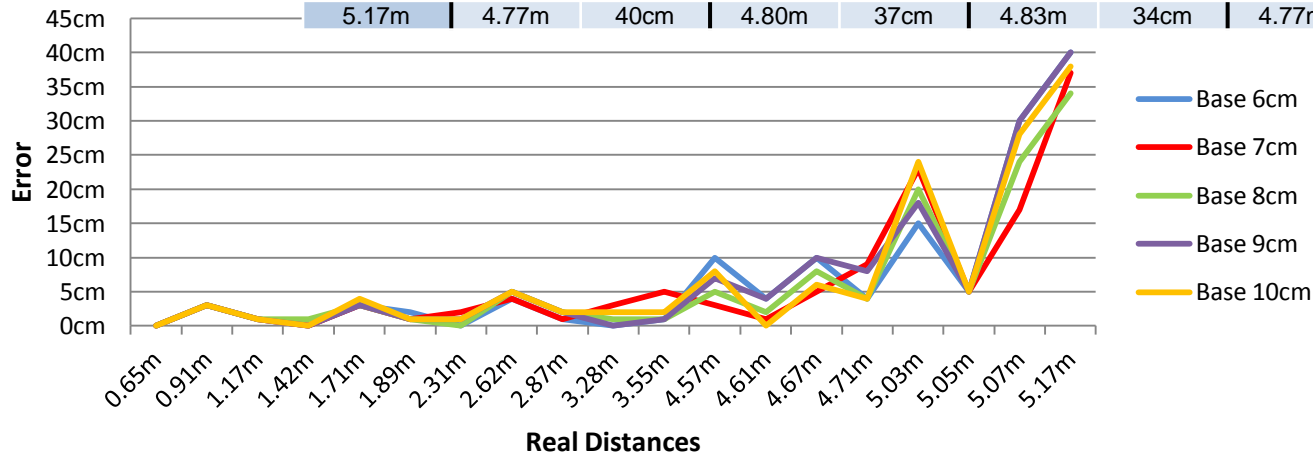


# Depth Estimation to Definite Points (Olympus)

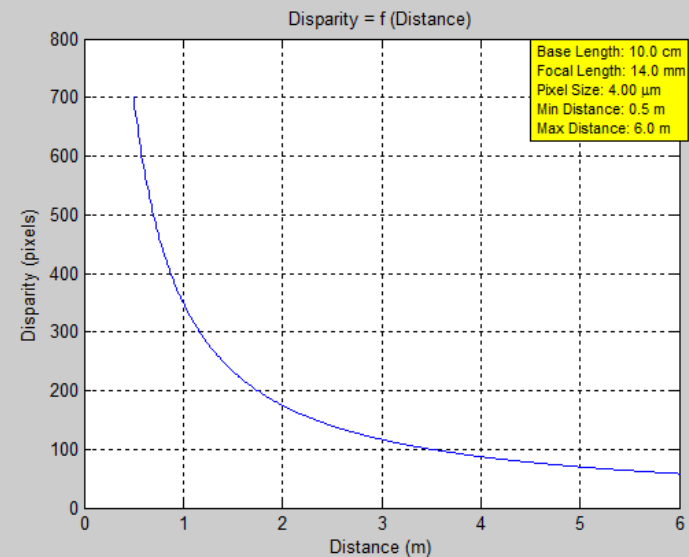
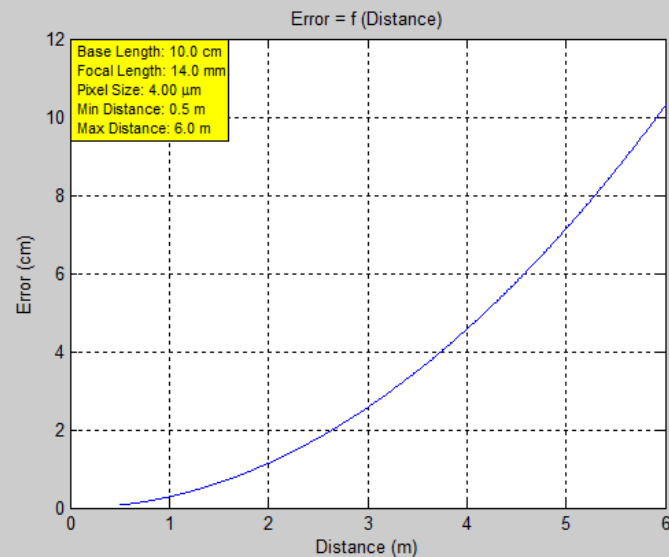
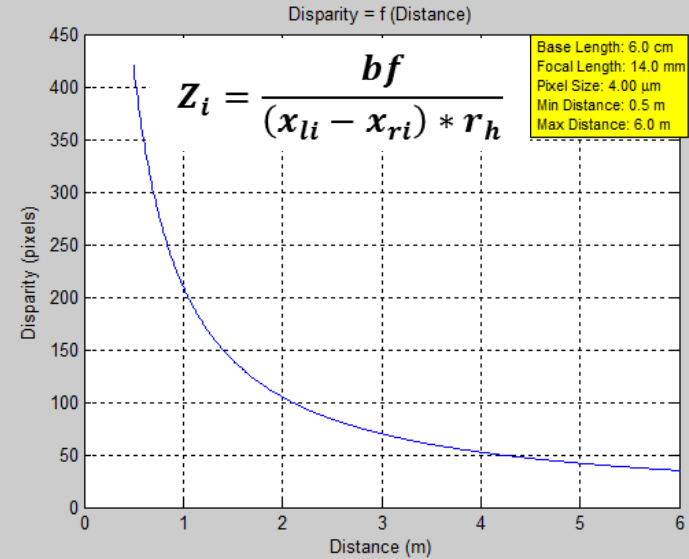
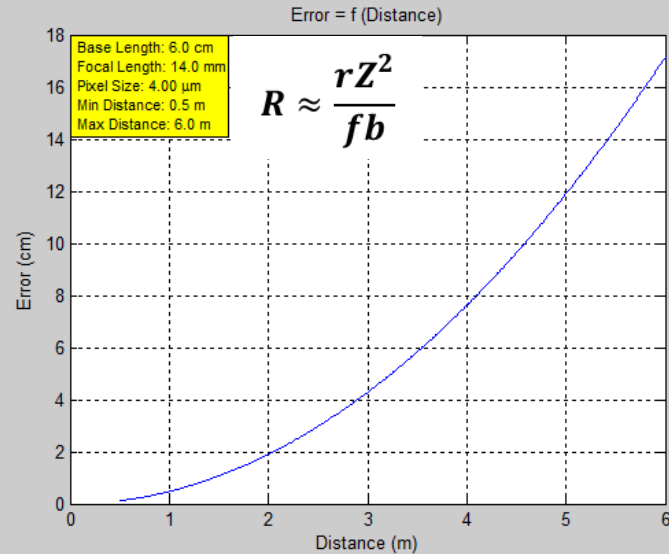


# Experimental Results (Olympus)

| Real Distance | Base length between cameras with focal length 14 mm |       |          |       |          |       |          |       |          |       |
|---------------|---|-------|----------|-------|----------|-------|----------|-------|----------|-------|
|               | 6cm   |       | 7cm      |       | 8cm      |       | 9cm      |       | 10cm     |       |
|               | Estimate  | Error | Estimate | Error | Estimate | Error | Estimate | Error | Estimate | Error |
| 0.65m         | 0.65m   | 0cm   | 0.65m    | 0cm   | 0.65m    | 0cm   | 0.65m    | 0cm   | 0.65m    | 0cm   |
| 0.91m         | 0.88m   | 3cm   | 0.88m    | 3cm   | 0.88m    | 3cm   | 0.88m    | 3cm   | 0.88m    | 3cm   |
| 1.17m         | 1.18m   | 1cm   | 1.18m    | 1cm   | 1.18m    | 1cm   | 1.18m    | 1cm   | 1.18m    | 1cm   |
| 1.42m         | 1.42m   | 0cm   | 1.42m    | 0cm   | 1.41m    | 1cm   | 1.42m    | 0cm   | 1.42m    | 0cm   |
| 1.71m         | 1.74m   | 3cm   | 1.74m    | 3cm   | 1.74m    | 3cm   | 1.74m    | 3cm   | 1.75m    | 4cm   |
| 1.89m         | 1.91m   | 2cm   | 1.90m    | 1cm   | 1.90m    | 1cm   | 1.90m    | 1cm   | 1.90m    | 1cm   |
| 2.31m         | 2.31m   | 0cm   | 2.33m    | 2cm   | 2.31m    | 0cm   | 2.32m    | 1cm   | 2.30m    | 1cm   |
| 2.62m         | 2.66m   | 4cm   | 2.66m    | 4cm   | 2.67m    | 5cm   | 2.67m    | 5cm   | 2.67m    | 5cm   |
| 2.87m         | 2.88m   | 1cm   | 2.88m    | 1cm   | 2.89m    | 2cm   | 2.89m    | 2cm   | 2.89m    | 2cm   |
| 3.28m         | 3.28m   | 0cm   | 3.31m    | 3cm   | 3.29m    | 1cm   | 3.28m    | 0cm   | 3.30m    | 2cm   |
| 3.55m         | 3.56m   | 1cm   | 3.60m    | 5cm   | 3.54m    | 1cm   | 3.54m    | 1cm   | 3.57m    | 2cm   |
| 4.57m         | 4.47m   | 10cm  | 4.54m    | 3cm   | 4.52m    | 5cm   | 4.50m    | 7cm   | 4.49m    | 8cm   |
| 4.61m         | 4.57m   | 4cm   | 4.62m    | 1cm   | 4.59m    | 2cm   | 4.57m    | 4cm   | 4.61m    | 0cm   |
| 4.67m         | 4.57m   | 10cm  | 4.62m    | 5cm   | 4.59m    | 8cm   | 4.57m    | 10cm  | 4.61m    | 6cm   |
| 4.71m         | 4.67m   | 4cm   | 4.62m    | 9cm   | 4.67m    | 4cm   | 4.63m    | 8cm   | 4.67m    | 4cm   |
| 5.03m         | 4.88m   | 15cm  | 4.80m    | 23cm  | 4.83m    | 20cm  | 4.85m    | 18cm  | 4.79m    | 24cm  |
| 5.05m         | 5.00m   | 5cm   | 5.00m    | 5cm   | 5.00m    | 5cm   | 5.00m    | 5cm   | 5.00m    | 5cm   |
| 5.07m         | 4.77m   | 30cm  | 4.90m    | 17cm  | 4.83m    | 24cm  | 4.77m    | 30cm  | 4.79m    | 28cm  |
| 5.17m         | 4.77m   | 40cm  | 4.80m    | 37cm  | 4.83m    | 34cm  | 4.77m    | 40cm  | 4.79m    | 38cm  |

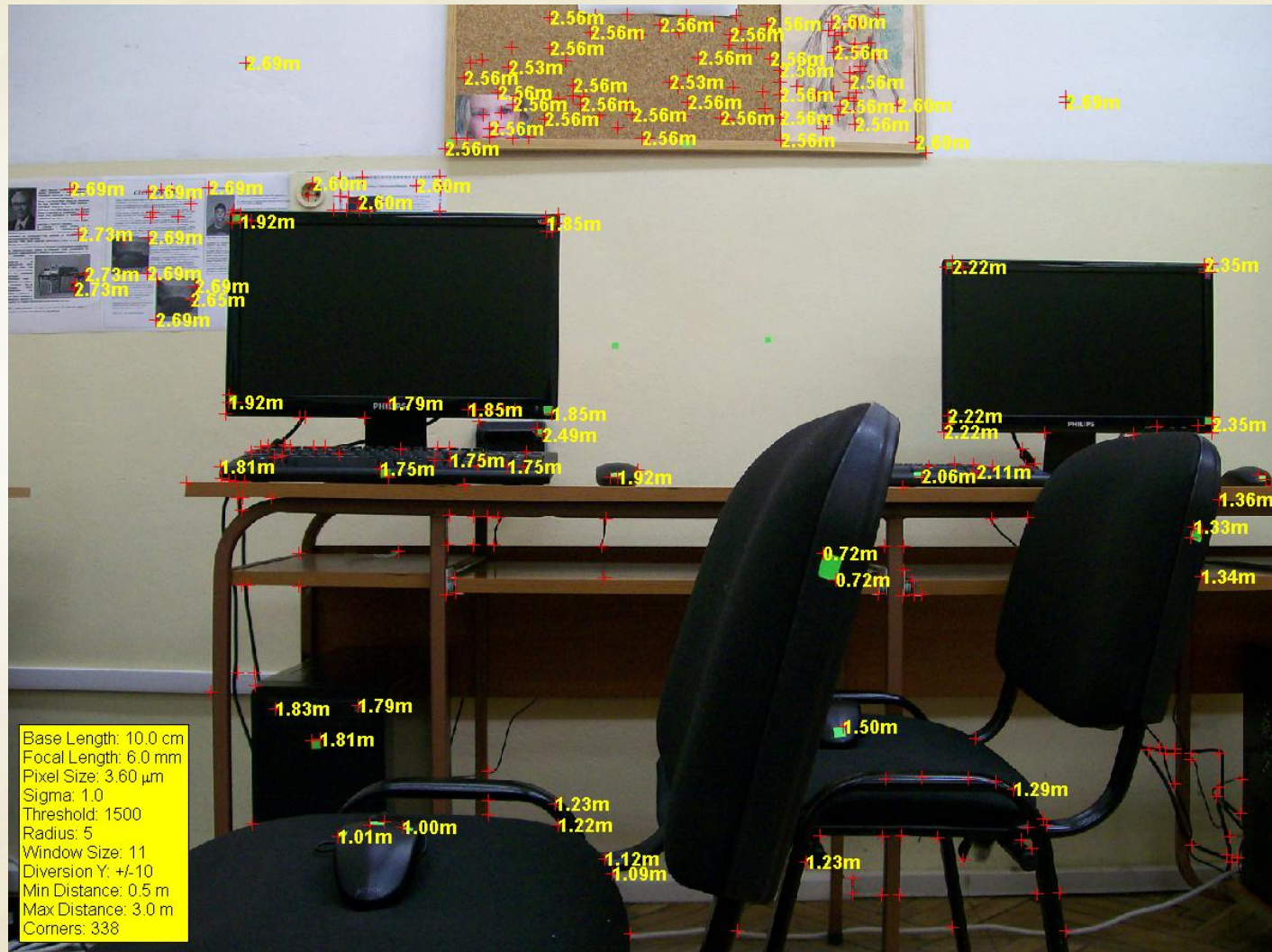


# Depth Resolution Error (Olympus)



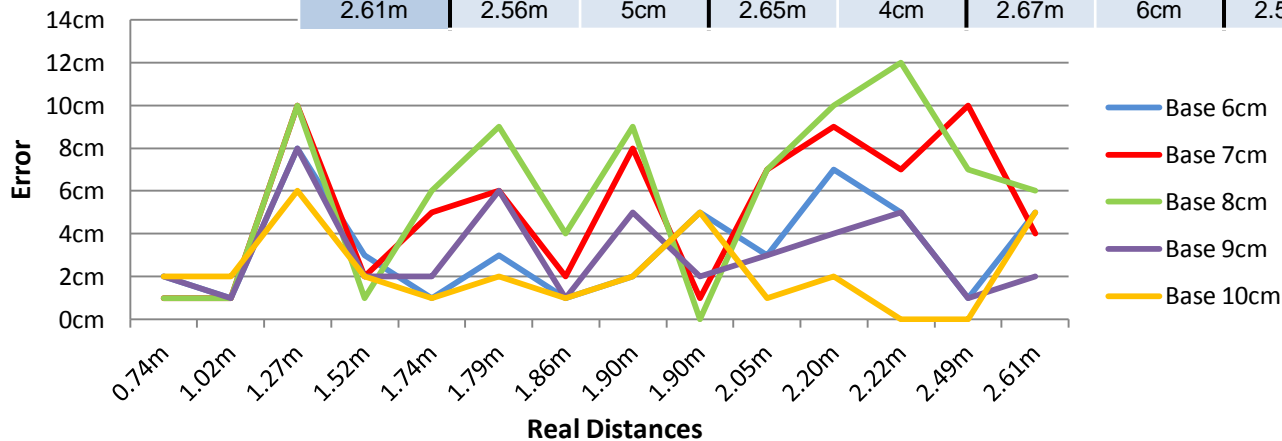


# Depth Estimation to Definite Points (Kodak)

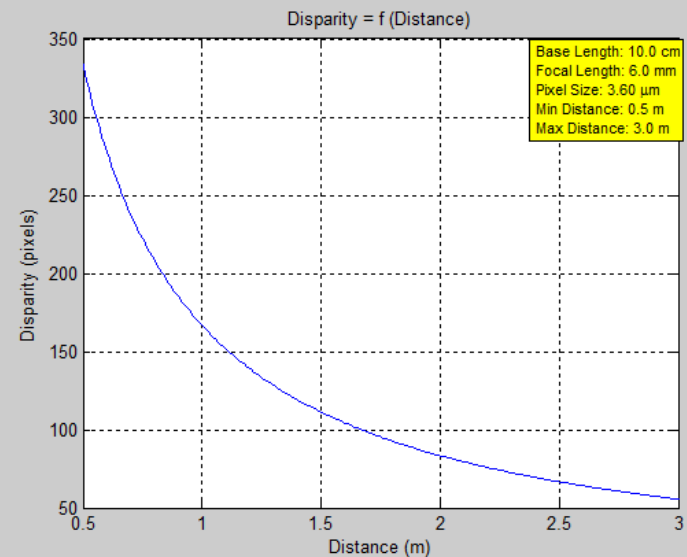
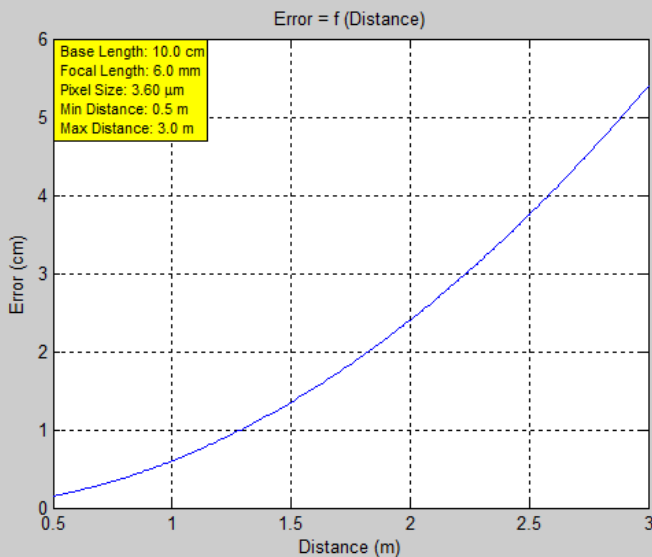
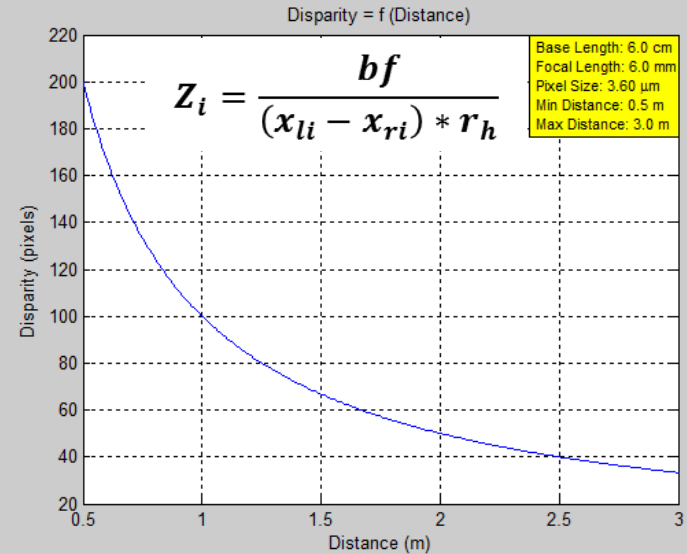
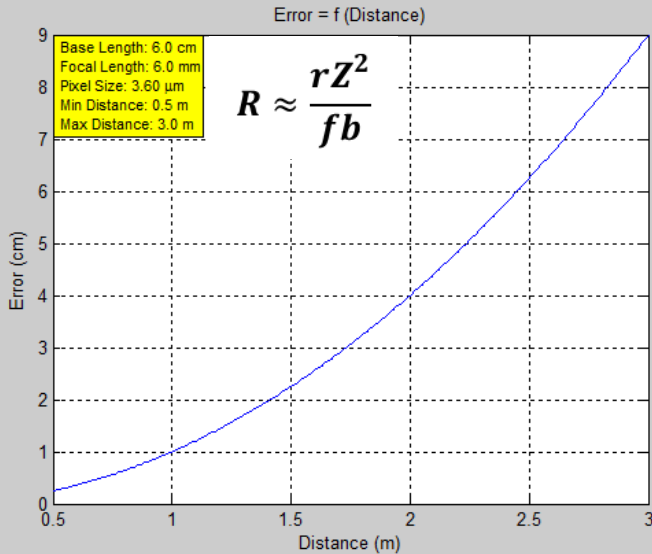


# Experimental Results (Kodak)

| Real Distance | Base length between cameras with focal length 6mm |       |          |       |          |       |          |       |          |       |
|---------------|---|-------|----------|-------|----------|-------|----------|-------|----------|-------|
|               | 6cm   |       | 7cm      |       | 8cm      |       | 9cm      |       | 10cm     |       |
|               | Estimate  | Error | Estimate | Error | Estimate | Error | Estimate | Error | Estimate | Error |
| 0.74m         | 0.72m   | 2cm   | 0.73m    | 1cm   | 0.73m    | 1cm   | 0.72m    | 2cm   | 0.72m    | 2cm   |
| 1.02m         | 1.01m   | 1cm   | 1.01m    | 1cm   | 1.03m    | 1cm   | 1.01m    | 1cm   | 1.00m    | 2cm   |
| 1.27m         | 1.35m   | 8cm   | 1.37m    | 10cm  | 1.37m    | 10cm  | 1.35m    | 8cm   | 1.33m    | 6cm   |
| 1.52m         | 1.49m   | 3cm   | 1.54m    | 2cm   | 1.53m    | 1cm   | 1.50m    | 2cm   | 1.50m    | 2cm   |
| 1.74m         | 1.75m   | 1cm   | 1.79m    | 5cm   | 1.80m    | 6cm   | 1.76m    | 2cm   | 1.75m    | 1cm   |
| 1.79m         | 1.82m   | 3cm   | 1.85m    | 6cm   | 1.88m    | 9cm   | 1.85m    | 6cm   | 1.81m    | 2cm   |
| 1.86m         | 1.85m   | 1cm   | 1.88m    | 2cm   | 1.90m    | 4cm   | 1.85m    | 1cm   | 1.85m    | 1cm   |
| 1.90m         | 1.92m   | 2cm   | 1.98m    | 8cm   | 1.99m    | 9cm   | 1.95m    | 5cm   | 1.92m    | 2cm   |
| 1.90m*        | 1.85m   | 5cm   | 1.91m    | 1cm   | 1.90m    | 0cm   | 1.88m    | 2cm   | 1.85m    | 5cm   |
| 2.05m         | 2.08m   | 3cm   | 2.12m    | 7cm   | 2.12m    | 7cm   | 2.08m    | 3cm   | 2.06m    | 1cm   |
| 2.20m         | 2.27m   | 7cm   | 2.29m    | 9cm   | 2.30m    | 10cm  | 2.24m    | 4cm   | 2.22m    | 2cm   |
| 2.22m         | 2.27m   | 5cm   | 2.29m    | 7cm   | 2.34m    | 12cm  | 2.27m    | 5cm   | 2.22m    | 0cm   |
| 2.49m         | 2.50m   | 1cm   | 2.59m    | 10cm  | 2.56m    | 7cm   | 2.50m    | 1cm   | 2.49m    | 0cm   |
| 2.61m         | 2.56m   | 5cm   | 2.65m    | 4cm   | 2.67m    | 6cm   | 2.59m    | 2cm   | 2.56m    | 5cm   |



# Depth Resolution Error (Kodak)





# Conclusion and Future Work

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- The accuracy of the investigated method for determining distance to given objects in a static scene by precise horizontal translation of one camera can be viewed from physical and algorithmic point:
  - For the physical accuracy improvement a subjective adjustments (like choice of optimal base and focal length, knowledge for optical distortions) need to be applied, in order to calibrate the stereovision system, according to the working distance range.
  - The algorithmic accuracy aspect depends on the software methods for determining the feature points (corners) and their correspondence.
- The future development of the investigated method can be focused on:
  - ✓ As much as possible points from the stereoimages to be viewed as a characteristic and their correspondence to be found in the other image;
  - ✓ Determining the 3D coordinates of a random characteristic point;
  - ✓ The distance determining algorithm to be improved to work with arbitrary translation and rotation between the cameras (or maybe a single camera?);
  - ✓ 3D Object Recognition;
  - ✓ 3D Video Stabilization.

**THANK YOU FOR YOUR  
QUESTIONS**

**(before PART 2)**

# 2D Real-Time Video Stabilization - Introduction

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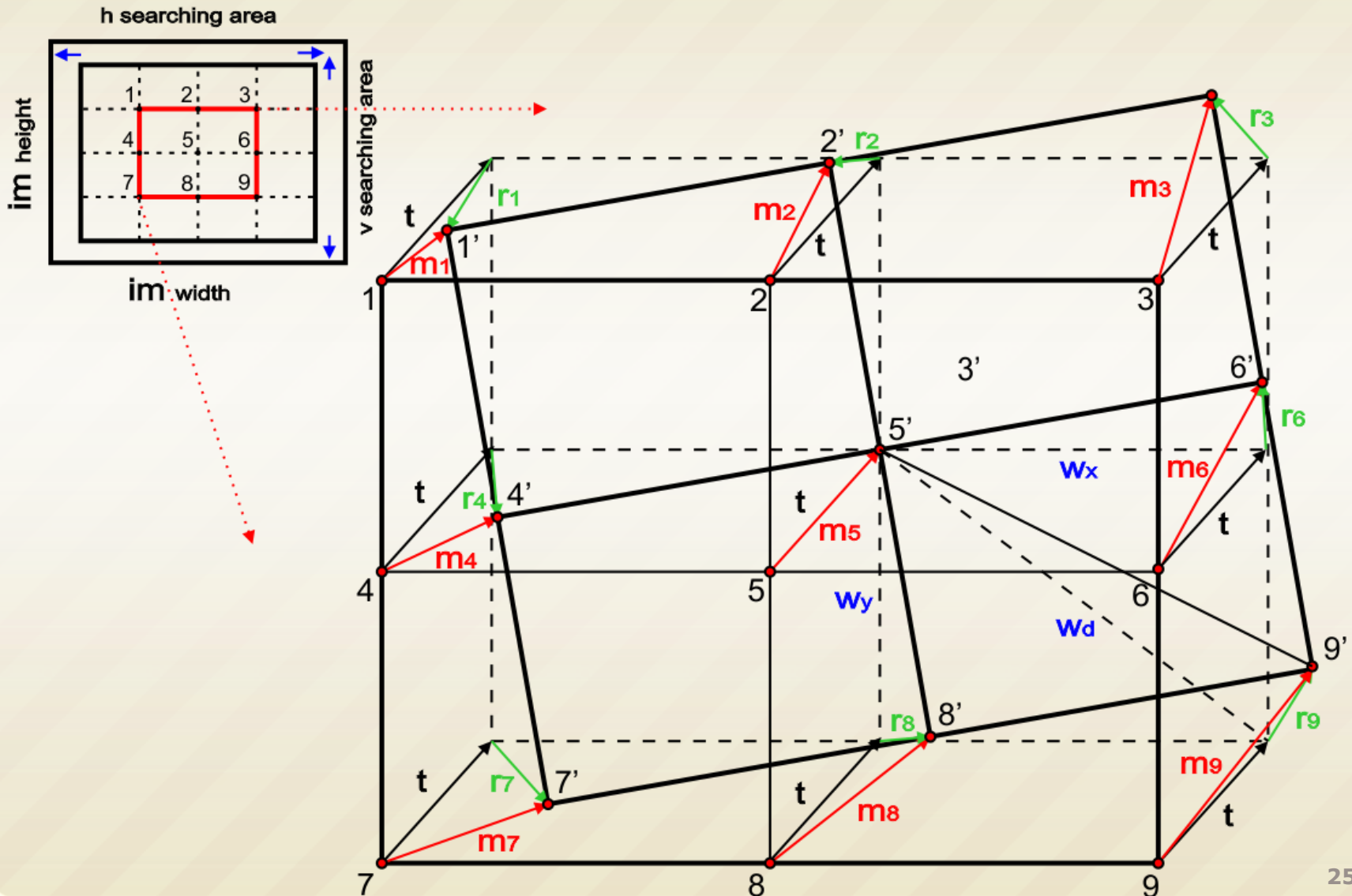
- Video stabilization seeks to create a stable version of casually shot video (usually filmed on a handheld device, such as a mobile phone or a portable camcorder) which is typically shaky and undirected.
- 2D video stabilization techniques work by estimating a 2D motion model between consecutive frames and applying per-frame warps between the original and filtered motion models.
- In case of approximately planar scenes (with an arbitrary camera movement) or cases where the camera shake is strictly rotational (within an arbitrary scene), unwanted jitters can be effectively reduced based on two-dimensional reasoning of the video.
- Assuming the scene geometry and camera motion do fall into these categories, such 2D stabilization methods are robust, operate on the entire frame, require a small number of tracked points and consume minimal computing efforts.
- This type of stabilization became very common in still and video cameras where it is implemented via mechanical means, either in the lens or the camera sensor.

# An Algorithm for 2D Video Stabilization

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- 1) Motion Vectors Model;
- 2) Estimating Horizontal and Vertical motion vectors for each block between Next and Previous frame by the method of *SAD*;
- 3) 1<sup>st</sup> Solving a Linear System of 18 equations with 4 unknowns by the *Least Square Method*;
- 4) Eliminating equations with values outside  $1.5 * \text{standard deviation} (\text{const} * \sigma)$ ;
- 5) 2<sup>nd</sup> Solving a Linear System with less or equal number of equations with 4 unknowns by the *Least Square Method*;
- 6) Determining the interframe translational and rotational vectors based on the 2<sup>nd</sup> LSM;
- 7) Smoothing Global H/V/R Motion.

# Motion Vectors Model



# Example of Given Previous Frame



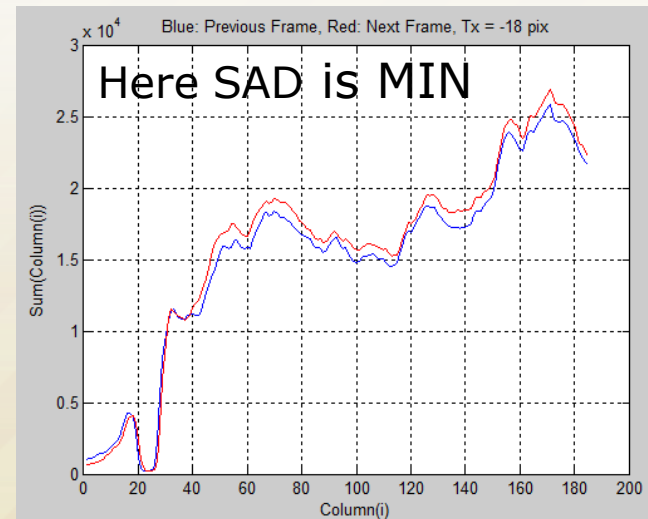
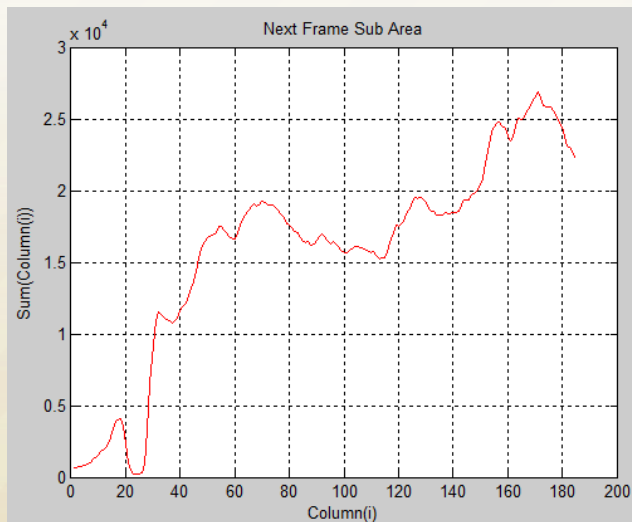
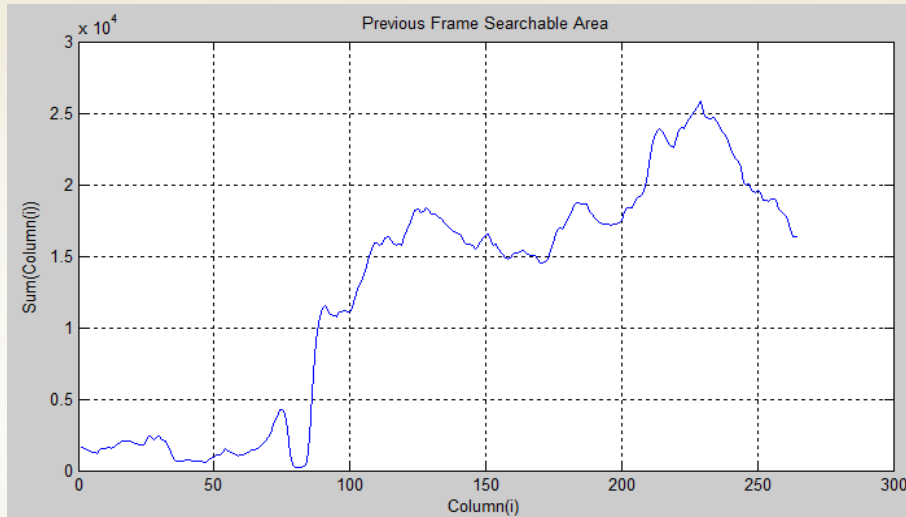


# Example of Given Next Frame



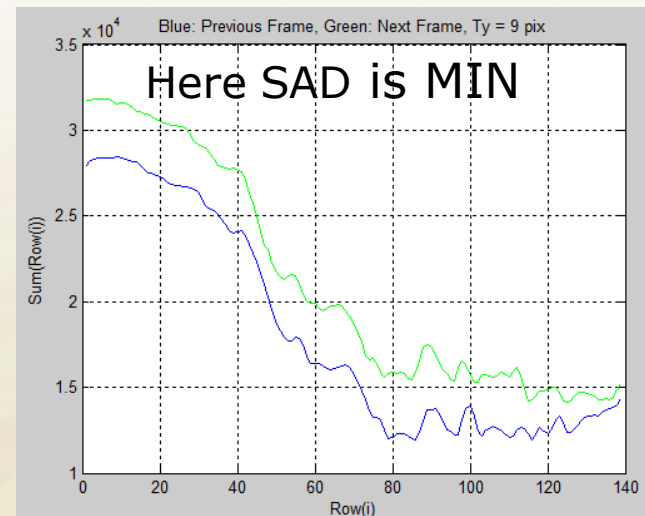
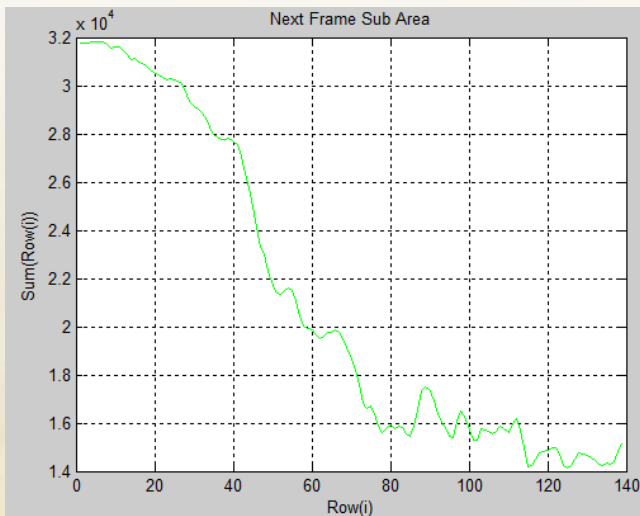
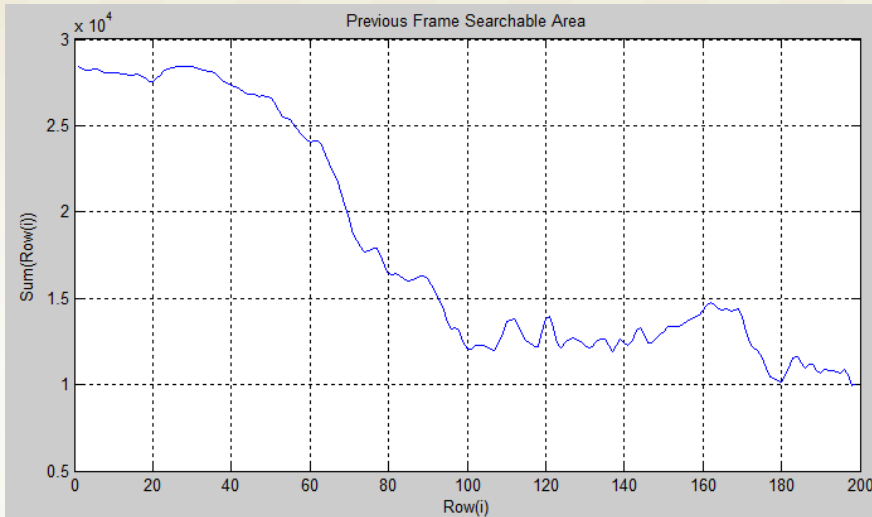
# Example of SAD between 1<sup>st</sup> areas

## Horizontal Searching




# Example of SAD between 1<sup>st</sup> areas

## Vertical Searching



# Live Demo

 2D Video Stabilization 1.1

**Smoothing Movements**

Middle of Gaussian  ☒ Smooth Angle

☐ Draw Angle  
☐ Draw Horizontal Translation  
☐ Draw Vertical Translation

**Show Transformations**

Between  And  Frame

☒ Show Previous Frame  
☒ Show Next Frame  
☒ Show Back Transformed Frame

**Converting Frames To Video**

Frame Rate  fps  
Compression

From  To  Frames

**Correlation**

Type  ☒ Intensity Invariant (AVG)

Correlation of  Region

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

Between  And  Frame

**Important Parameters**

Sigma For The LSM   
Overlapping 1/

☐ Correct Translation Only  
☒ Show/Save Color Images

**Controlling I/O Frames**

Frame    
  
Rotation Limit  Deg

# Conclusion

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- Limitations of the 2D Video Stabilization:
  - In cases where the scenes contain objects at arbitrary depths, a full-frame warp cannot model the parallax that is induced by a translational shift in viewpoint and this level of scene modelling is insufficient for video stabilization.
  - The second limitation of 2D motion models is that there is no knowledge of the 3D trajectory of the input camera, making it impossible to simulate an idealized camera path similar to what can be found in professional tracking shots.
- The 3D Video Stabilization could overcome these limitations:
  - Using structure-from-motion technique (where a sparse set of feature points along the video are tracked and their correspondences are used) to recover the 3D camera pose and the 3D location of every feature point.
  - Estimating 2D feature trajectories from the input video (using the standard KLT approach), smooth them and synthesize new frames by video warping.
  - Other techniques use: Epipolar Geometry, L1 optimal camera path, etc.

**THANK YOU**